# **FUNDAMENTALS OF CALCULUS**

# AND

# RASONING

# FOR CLASS-XI &XII CBSE SYLLABUS

## A CONTEMPORARY APPROACH

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